- 1 Beyond the Active Site: The addition of a remote loop reveals a new complex
- 2 biological function for chitinase enzymes.
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13 Abstract

14 Loops are small secondary structural elements that play a crucial role in the emergence of new 15 enzyme functions. However, our understanding of loop functions is mainly limited to the catalytic loops. To understand the function of remote loops in enzymes, we studied Glycoside 16 17 hydrolase family 19 (GH19) chitinase - an essential enzyme family for pathogen degradation 18 in plants. By revealing the evolutionary history and loops appearance of GH19 chitinase, we 19 discovered that one loop which is remote from the catalytic site, is necessary to acquire the 20 new antifungal activity. We demonstrated that this remote loop directly accesses the fungal cell 21 wall, and surprisingly, it needs to adopt a defined structure supported by long-range 22 intramolecular interactions to perform its function. Our findings prove that Nature applies this 23 new strategy at the molecular level to achieve a complex biological function while maintaining 24 the original activity one in the catalytic pocket, suggesting an alternative way to design new 25 enzyme function.

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30 Introduction

Protein evolution is an essential process that drives diversity in nature by enabling the 31 32 emergence of new functions¹. Understanding how protein evolves is fundamental, not only for unraveling the natural diversification of proteins but also for designing new protein functions 33 in vitro. The structure of more than 30,000 proteins reveals that nature uses a limited number 34 35 of basic structures (scaffolds) to achieve an enormous variety of functions². Indeed, many reports demonstrate that this diversity is often acquired by diversifying the flexible catalytic 36 37 loop structures exposed on the protein's surface, while preserving the robust scaffold and the active site residues common among the enzyme family as core structures^{3–5}. For instance, 38 altering catalytic specificity by grafting $loop^6$ or shaping the catalytic activity *via* mutations in 39 40 the catalytic loop⁷. These strategies are a major source of structural and functional variation within protein superfamilies⁸. Thus, mutations in the catalytic loop regions have garnered 41 42 significant attention because they can directly impact function. Indeed, because of their functional roles like ligand binding⁹, promoting function via conformational changes¹⁰, and 43 functional switching¹¹, the propensity of loop regions to acquire mutations is evolutionarily 44 45 advantageous. However, while previous studies have extensively explored the catalytic loops^{6,71213}, the role of functional remote loop regions remains unexplored. 46

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To understand how nature acquires new functions *via* remote loops, we investigated the evolution of Glycoside Hydrolase family 19 chitinases (GH19 chitinase; EC 3.2.1.14). GH19 chitinase hydrolyzes the glycosidic bonds of chitin, namely beta-1, 4-linked *N*-acetyl-Dglucosamine. Chitin is the main component of exoskeletons and cell walls of various organisms, including arthropods and fungi. Despite lacking an endogenous substrate for plant chitinases, many plants synthesize various chitinases. One of the physiological roles of chitinase is to 54 defend plants against pathogenic fungi by degrading chitin, a major component of the cell wall of many fungi¹⁴. Interestingly, even in GH19 chitinases, some chitinases do not exhibit 55 antifungal activity. Taira *et al.* reported a difference in the antifungal activity of two chitinases 56 57 from plants¹⁵, - in this work, we will call them loopless and loopful GH19 chitinases. Comparing the sequences and the structures of both GH19, the catalytic residues and the core 58 structure that consists of the catalytic cleft are conserved. However, loopful GH19, a chitinase 59 60 from rye seed, contains six loop regions, whereas loopless GH19, a chitinase from moss, lacks five of those loop regions seen in loopful GH19 (Fig. 1A and B). Interestingly, loopful GH19 61 62 exhibits antifungal activity against the fungi Trichoderma sp., while loopless GH19 does not¹⁵. However, it is unclear how chitinase could achieve a gain in antifungal activity without any 63 apparent effect on catalytic activity. 64

65 Herein we investigated the evolution of GH19 chitinase to understand how functional 66 innovation occurred. We inferred five ancestral proteins with different loop combinations in 67 remote loop regions. By characterizing these proteins variants, we discovered that loop II is 68 critical for acquiring antifungal activity. Using structural analysis, molecular dynamics 69 simulations, and computational studies, we showed that this remote loop allows new function 70 through fine-tuned intramolecular interactions. Imaging studies via fluorescence microscope experiments unraveled that the acquisition of remote loop II access the substrate in a new 71 72 specific cellular location, the fungal cell wall. This is the first report that highlights how Nature 73 acquired remote loops in a protein structure to access a new and complex biological function.

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75 **Results**

Phylogenetic analysis reveals the emergence of antifungal activity in GH19 chitinase. To
identify the remote loop regions acquisition that played a role in the emergence of antifungal
activity and when such an acquisition occurred in GH19 chitinase, we performed phylogenetic

79 analysis and ancestral sequence reconstruction. After extensive collection of all available sequences belonging to GH19 chitinase from plants and the removal of redundancy, we 80 81 inferred the maximum-likelihood phylogenetic tree of 179 GH19 chitinase sequences. We used 82 ancestral protein reconstruction to infer the most likely amino acid sequence for each ancestral node in the phylogeny. To avoid the bias that phylogenetic classification is affected by the 83 84 presence or absence of loop regions, we inferred two phylogenetic trees using a multiple 85 sequence alignment (MSA) of the collected sequences, and a MSA modified by removing the 86 six loop regions in question. After we confirmed that the tree topology did not change based 87 on the presence/absence of loop regions in the MSA (Fig. S2 and S3), we used the tree based on the unmodified MSA and selected five ancestral nodes where InDels of the loop regions 88 occurred, designated Anc1 to Anc5 based on the presence/absence of loop regions in the extant 89 90 sequences (Fig. 1C). We experimentally characterized chitinase activities and antifungal 91 activities of five reconstructed ancestral proteins and two extant GH19 sequences. All five 92 ancestral proteins showed a similar level of chitinase activity to the two modern GH19 93 chitinases (Table 1), while Anc5 also exhibited antifungal activity. Anc1-4 did not exhibit antifungal activity (Fig. 1D), suggesting that antifungal activity seems to be acquired during 94 95 the transition from Anc4 to Anc5.

Characterization of the functional intermediates between Anc4 and Anc5. To identify the 96 key loop insertion for antifungal activity acquisition, we constructed six variants of two 97 98 reconstructed ancestral proteins, Anc4 and Anc5 with different combinations of loop I and II 99 (Anc4 + Loop I, Anc4 + Loop II, Anc4 + Loop I and II, Anc5ΔLoop I, Anc5ΔLoop II, and 100 Anc5 Δ Loop I and II). We experimentally characterized antifungal activities and hydrolytic 101 activities of these variants. To compare the strength of their antifungal activities, we calculated 102 IC₅₀ by performing a hyphal re-extension inhibition assay. Addition/removal of loop I and/or 103 II regions did not affect their hydrolytic activities (1.1 - 1.5 - fold) except for in the case of loop

I addition to Anc4. Insertion of loop I to Anc4 resulted in a loss of catalytic activity of Anc4
(Fig. 2B). However, removing loop II from Anc5 decreased its antifungal activity by 12-fold
while removing loop I did not influence its antifungal activity (roughly 1.02-fold increase, Fig.
2B). These results strongly suggest that loop II has a role in enhancing antifungal activity.
However, it is worth noting that the addition of loop II to Anc4 did not improve its antifungal
activity. Anc4 and 5 differ by 45 substitutions (Fig. 2A, C), suggesting that loop II enhances
antifungal activity in combination with residues in the protein scaffold.

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Structural analysis of Anc4 and Anc5 and molecular dynamics (MD) simulations revealed the importance of long-range interactions in the emergence of antifungal activity.

To get structural insights into the emergence of antifungal activity in GH19 chitinase, we first 114 115 solved the X-ray crystal structure of Anc4 and Anc5 (Table S3). Overall, the backbone structures of Anc4 and Anc5 were nearly identical (RMSD of $C\alpha = 0.478$ Å) and the orientation 116 of catalytic residues is similar, suggesting that loop I and II addition/removal did not cause 117 major structural disruptions. This is supported by the fact that addition/removal of loop I and/or 118 119 II regions did not affect their hydrolytic activities except for the loop I insertion into Anc4. The 120 loss of the hydrolytic activity in Anc4 via loop I insertion might be due to the lack of disulfide bonding between loop I and the core scaffold. This is because the cysteine residue that forms 121 122 the disulfide bonding with loop I is replaced by another residue (Val 81 in the MSA, Fig. S5). Although Anc4 and Anc5 showed no significant structural difference and their mutants Anc4 123 124 + Loop II and Anc5 Δ Loop I had similar hydrolytic activity, their antifungal activities were significantly different (Anc5 Δ Loop I showed 56-fold higher activity than Anc4 + Loop II). 125 Therefore, we explored the contributions of protein dynamics to the acquisition of antifungal 126 activity by performing molecular dynamics (MD) simulations. We performed four runs of 200 127 ns simulations of the model structure of Anc4 + Loop II and Anc5∆Loop I built using Anc4 128

129 and Anc5 structures (PDB 8HNE and 8HNF). In Anc5∆Loop I, the simulation showed reduced 130 mobility of the loop II regions and a loop region between the ninth and tenth α -helices 131 (positions 192 - 201) compared to Anc4 + Loop II (Fig. 3A, B). Some of the 45 substitutions support the stabilization of loop II in Anc5∆Loop I. Structural comparison of Anc4 and Anc5 132 revealed six substitutions forming new interactions with loop II regions (Fig. 3C). Two 133 substitutions, P12K and N13H, formed new hydrogen bonding with Asp residue in loop II. The 134 135 His 13 residue is also involved in hydrophobic interaction with Trp residue in loop II (Fig. 3C). 136 D197(217)R (residue numbers in Anc5 state are in parentheses) substitution formed new 137 hydrogen bonds between the N terminus and the tenth α -helix (Fig. 3C). N193(213)G 138 substitution reduced structural hindrance with the Tyr residue in loop II (Fig. 3C). Loop II 139 insertion into Anc4 caused a change in conformational orientation of Ser 58, leading to a 140 formation of a hydrogen bond between the oxygen atom of Ser 58 and the nitrogen atom of the 141 Gly 60 as seen between Thr 65 and Gly 67 in Anc5. Y194(214)F substitution reduced structural 142 hindrance with the oxygen atom of Thr 65 (Fig. 3C). These substitutions are important for 143 stabilizing the loop II region to perform antifungal activity.

To assess whether residues in the scaffold have long-range effects on rigidity and 144 145 conformational modifications of loop II, we utilized rigidity transmission allostery (RTA) algorithms¹⁶. RTA is a computational approach based on mathematical rigidity theory^{17,18} and 146 147 graph theory, which analyzes long-range communication and allosteric networks within protein 148 structures^{19–22}. RTA measures whether local mechanical perturbation of rigidity at one site propagates and modifies rigidity and conformational degrees of freedom at distant site(s) in 149 150 protein structure. Starting with a structure, RTA first utilizes the method Floppy Inclusion and 151 Rigid Substructure Topography (FIRST)²³ to generate a constraint network, where protein structure is modeled in terms of vertices (atoms) and edges (i.e., covalent bonds, electrostatic 152 153 bonds, hydrogen bonds, and hydrophobic contacts). Every potential hydrogen bond is ranked

154 and assigned energy strength according to its donor-hydrogen-acceptor geometry. Upon rigidification of individual site(s) (i.e. residues), RTA then quantifies transmission (changes) 155 156 of degrees of freedom and strength of communication across protein structure. RTA analysis 157 on Anc5 Loop I showed that several residues in the scaffold are involved in long-range communication with loop II, revealing an allosteric network of residues that transmit 158 159 communication with loop II (Fig. 3D). Interestingly, many of the substitution residues are part of this communication network, suggesting they impact the stability and conformational 160 161 dynamics of loop II. To further probe this, we applied FIRST and decomposed the protein structures into rigid and flexible regions. FIRST rigid cluster decomposition on Anc4 + Loop 162 II and Anc5\[]Loop I structures predicted that loop II is stabilized by intra-hydrogen bonding 163 between the Pro 72 and the Asp 73 (residue number is based on the MSA in Fig. S5A), which 164 165 is observed only in Anc5∆Loop I structure (Fig. S5C). This results in a strong rigid cluster in 166 Anc5 Δ Loop I which persists over wide hydrogen bond energy strengths (Fig. S5D, E).

Loop II leads to gain of antifungal activity by promoting binding to the fungal cell wall. 167 To understand the complex biological role of loop II, we performed fluorescence microscope 168 experiments. These experiments aimed at verifying if the acquisition of loop II in GH19 169 170 chitinase plays a role in binding to the surface of the fungal cell wall. For this purpose, we prepared the catalytically inactive mutants of Anc4, Anc4 + Loop II, Anc5, Anc5 \(Loop I, \) 171 172 Anc5 Δ Loop II, and Anc5 Δ Loop I and II by replacing catalytic glutamate residue with 173 glutamine (The Glu 67 in the MSA, Fig. S2). This mutation makes proteins lose chitin degrading activity in the fungal cell wall. These inactive mutants were tagged with 174 175 AlexaFluor488. By fluorescence microscope experiments, we observed that only Anc5 and Anc5∆Loop I bound to the surface of fungal hyphae (Figs. 4 and S6). This result is consistent 176 with the result that Anc5 and Anc5 Δ Loop I showed 28-fold stronger antifungal activity than 177

Anc4 (Fig. 2b), suggesting that the acquisition of loop II is necessary to access the substrate inthe cell wall of fungi to perform antifungal activity.

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181 Discussion

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183 Proteins use the limited numbers of folds and have evolved their structure and function using substitutions and insertions and deletions (InDels) of loops and other secondary structures^{24,25}. 184 However, most studies focused on substitutions and InDels are rarely considered. In these rare 185 186 cases, when InDels are studied, they consist of one to three amino acid removal or addition^{26,27} or graft of the catalytic loops^{6,7,12}. Shining light on the roles of insertion or deletions of entire 187 188 remote loop regions in protein evolution can provide further understanding of how we can 189 engineer new protein functions. Our study reveals the molecular mechanism of an enzyme, 190 through addition of a remote loop, can acquire a new distinct function distant from the catalytic 191 site while maintaining its original activity.

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To address this, we first identified the transition where the remote loop regions were inserted 193 194 or deleted during evolution of the enzyme. This is the first study, to out best knowledge, that 195 demonstrates that phylogenetic analysis and ancestral sequence reconstruction can explore 196 remote loop acquisition in enzymes and thus identify potential hotspots for loop engineering. Most studies using ancestral sequence reconstruction have been performed with a fixed length 197 198 of multiple sequence alignment due to the ambiguous evolutionary information of InDels. In 199 our case, the function of GH19 chitinase varies from chitinase activity to antifungal activity, 200 depending on the presence/absence of remote loop regions. Our phylogenetic analysis with two 201 multiple sequence alignments (with/without the considered loop regions) showed that InDels 202 of remote loop regions did not occur frequently and the tree topology did not change

significantly due to the InDels of remote loop regions (Fig. S3). Thus, we identified the ancestral nodes where the protein acquired/lost remote loops and inferred functional ancestral proteins with different loop combinations (InDels). As previous studies^{27–29} demonstrated that InDels in loop regions are highly tolerated, our ancestral proteins showed robustness to add/remove loops. Thus, we demonstrate that ancestral sequence reconstruction approach in enzyme family with structural variations in loop regions is useful for designing enzyme with different loop combinations and exploring the potential remote site for loop engineering.

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211 Surprisingly these ancestral proteins have the same sequence length and almost identical structure (RMSD of $C\alpha = 0.478$ Å), however, they showed significantly different 212 213 antifungal activity (Anc4 + Loop II and Anc5 Δ Loop I), indicating that structural dynamics play an important role for the additional functions³⁰. In the evolution of GH19 chitinase, 214 215 stabilizing the key remote loop regions is important to perform new protein functions, and this 216 stabilization requires additional substitutions. Even if the order in which InDels or substitutions 217 occurred is not a trivial task, previous studies suggest that drastic mutational steps occur in combination with substitutions^{6,7,31}. 218

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220 In the evolution of GH19, it is interesting to note that the enzyme became dual-221 functional with a new complex biological activity while maintaining its original activity even though a trade-off between the catalytic activities to original substrate and the promiscuous 222 substrate is often observed in protein evolution³²³³. Trade-off can be associated with a change 223 224 in the conformational dynamics of the catalytic pocket optimizing to the substrate³⁰, and 225 bifunctionality can be achieved when this trade-off is weak enough to maintain original activity³⁴. In the case of GH19, there is no significant change in the dynamics near the catalytic 226 227 residues due to the mutations and original catalytic activities retained (Figs. 2B, 3A, and S5).

Thus, the enzyme seems to have developed a dual-function rather than expanding itspromiscuous activity.

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231 Strikingly, our findings show that the key loop insertion allowed the accessibility to the substrate in a different cell types and cellular location (Fig. 4). Since the target substrate for 232 antifungal activity is located in the cell wall of fungi, not in the solution, the protein needs to 233 234 access the substrate location to perform protein function. The fluorescence labeling experiments clearly show that chitinase access to the fungal cell wall to acquire antifungal 235 236 activity (Figs. 2B, 4, and S6). Nevertheless, the acquisition of this new and complex function 237 is possible only through the long-range interaction between the inserted secondary element and the substituted residues in the protein scaffold (Figs. 3 and S5). Herein we are the first to report 238 239 how remote loop insertion plays an important role in accessing the substrate.

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In addition, our findings are key to develop protein engineering methods aimed at accessing water-insoluble substrates such as cellulose, chitin, and plastic. To achieve efficient degradation of water-insoluble substrates, accessibility is equally important to catalytic efficiency³⁵. On the other hand, here, we are the first to prove how functional peptide grafting is not only limited to catalytic loop, but it can be extended to remote loops. In conclusion, we show an alternative and effective way to redesign or expand enzyme function, opening new ways of thinking for enzyme designers.

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249 Methods

250 *Phylogenetic analysis and ancestral sequence reconstruction*

251 2617 sequences of plant GH19 chitinase were collected from the UniProtKB database³⁶.

252 Redundant sequences with more than 50% sequence identity were filtered using the CD-HIT

253 program. The resulting 682 sequences were aligned using MAFFT ver. 7³⁷. Only GH19 catalytic domain sequences were aligned, and additional domains were manually removed 254 using an alignment visualizing software, Aliview³⁸. Sequences of a loopless type GH19 255 256 chitinase from Gemmabryum coronatum (Uniprot: A9ZSX9; residues 25-228) and a loopful type GH19 chitinase from Secale cereale (Uniprot: Q9FRV0; residues 24-266) were used as 257 references for the smallest and largest GH19 catalytic domain, respectively. 11 bacterial GH19 258 259 chitinase sequences were added to the dataset as an outgroup. The resulting 179 sequences were aligned with MAFFT and a maximum-likelihood phylogenetic tree was estimated using 260 261 the model (WAG+F+I+G4) automatically determined in IQ-TREE³⁹. Ancestral protein 262 sequences were reconstructed using the empirical Bayesian method applied by IQ-TREE³⁵. The ancestral sequences Anc1 to Anc5 were reconstructed using the WAG substitution matrix 263 264 together with the maximum-likelihood phylogenetic tree.

265

266 *Cloning and site-directed mutagenesis*

267 Codon-optimized genes encoding the ancestral GH19 chitinase proteins and loopful type GH19 chitinase from Secale cereale (Uniprot: Q9FRV0; residues 24-266) were synthesized by 268 TWIST Bioscience and cloned into the pET-22b (+) vector using the iVEC3⁴⁰. PCR 269 amplifications for synthetic genes and a linear-pET-22b (+) vector were performed with using 270 271 PrimeSTAR® Max DNA polymerase (TaKaRa) and the designed primers (Supplementary 272 Table 1) containing appropriate overlapping regions for iVEC3. The gene coding loopless type 273 GH19 chitinase from Gemmabryum coronatum (Uniprot: A9ZSX9; residues 25-228) cloned 274 into the pET-22b (+) vector was a gift from Toki Taira.

Site-directed mutagenesis was achieved by Inverse PCR using PrimeSTAR® Max DNA
polymerase (TaKaRa) with the designed primers (Supplementary Table 1). Successful cloning
and mutagenesis were confirmed by Sanger sequencing.

278

279 Protein expression and purification

E. coli SHuffle T7 (DE3) cells harboring the protein gene of interest were grown in LB at 37 °C 280 281 to OD₆₀₀ 0.6-0.8, induced with 0.1 mM β-d-1-isopropyl thiogalactopyranoside (IPTG) and incubated further for 24 hours at 18 °C. Cells were pelleted and stored at -80 °C before protein 282 purification. The cells were disrupted by sonication in a 20 mM Tris-HCl buffer, pH 8.0. The 283 284 sonicated extract was separated into soluble and insoluble fractions by centrifugation at 12,000×g for 15 minutes at 4 °C. The soluble fraction was dialyzed against 10 mM sodium 285 286 acetate buffer, pH 5.0, and filtered before applying to a RESOURCE Q column (6 mL, Cytiva) 287 or HiTrap SP HP column (5 mL, Cytiva) previously equilibrated with the same buffer. The elution was done with a linear gradient of NaCl from 0 to 0.3 M in the same buffer. The 288 289 recombinant protein fractions were collected and dialyzed against a 5 mM Tris-HCl buffer 290 containing 150 mM NaCl, pH 8.0. Purified recombinant proteins were concentrated using a Millipore centrifugal protein concentration device (10 kDa cutoff) and loaded onto a 291 292 Superdex200 Hiload 16/600 column (Cytiva) equilibrated with 5 mM Tris-HCl buffer containing 150 mM NaCl, pH 8.0. Protein purity was confirmed by SDS-PAGE, and protein 293 concentrations were measured spectrophotometrically using molar absorption coefficients 294 calculated in ProtParam (http://expasy.org/tools/protparam.html). 295

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297 *Chitinase activity assay*

298 Chitinase activity was measured colorimetrically with glycol chitin as a substrate. Ten μ L of 299 the sample solution was added to 150 μ L of 0.2% (w/v) glycol chitin solution in 0.1 M sodium 300 acetate buffer, pH 5.0. After incubation of the reaction mixture at 37°C for 15 minutes, the 301 reducing power of the mixture was measured with ferric ferrocyanide reagent by Imoto &

302 Yagishita⁴¹. One unit of activity was defined as the enzymatic activity that produced 1 mmol
303 of GlcNAc per minute at 37°C.

304

305 Antifungal activity assay

306 *Qualitative assay*

An antifungal assay was performed according to the method of Schlumbaum *et al.*¹⁴ with modification. An agar disk (4 mm in diameter) containing the test fungus, *T. longibrachiatum*, prepared from the cultured fungus on potato dextrose broth with 1.5% (w/v) agar (PDA), was placed in the center of a Petri dish containing PDA. Wells were subsequently punched into the agar at a 15 mm distance from the center of the Petri dish. 500 pmol of each protein sample was placed into the wells. The plates were incubated for 24 hours at 25°C.

313 *Quantitative assay*

314 Hyphal re-extension inhibition assay was done by using *T. longibrachiatum*. Agar disks (4 mm and 1 mm in diameter and in-depth, respectively) containing the fungal hyphae, which were 315 316 derived from the resting part of the fungus previously cultured on potato dextrose broth 317 containing 1.5% (w/v) agar (PDA), were put on another PDA plate with the hyphae attached 318 side down. Five µL of sterile water or sample solution were overlaid on the agar disks, and then the plate was incubated at 25 °C for 12 hours. After incubation, images of the plates were 319 320 scanned using an image scanner. The areas of the re-extended hyphae were calculated as 321 numbers of pixels by GNU Image Manipulation Program (GIMP, ver. 2.0). The protein 322 concentration required for inhibiting the growth of the fungus by 50% was defined as IC₅₀ and 323 determined by constructing dose-response curves (percentage of growth inhibition versus 324 protein concentration).

325

326 Differential scanning fluorimetry

Differential scanning fluorimetry (DSF) experiments were performed using StepOnePlus Instrument, a real-time PCR equipment. Reaction mixtures contained 2.5 μ M protein in 10 mM sodium acetate buffer, pH 5.0, 5× SYPRO orange dye in a total volume of 20 μ L and dispensed into a 96-well PCR plate. Fluorescence intensities were monitored continuously as the sample mixtures were heated from 20 °C to 99 °C at a rate of 1% (approximatelu 1.33 °C/min), using the ROX channel. Melting temperatures (T_m) were determined by fitting the fluorescence derivative data to a quadratic equation in the vicinity of the Tm in R software.

334

335 *Crystallization*.

After purification, Anc4 and Anc5 were concentrated at 10 mg/ml and 5.67 mg/ml in the 5 mM 336 Tris-HCl buffer, pH 8.0, respectively. Initial crystallization screens were performed using 337 338 various crystallization screening kits commercially available. The protein solution drop (0.4 mL) was mixed with 0.4 mL of a reservoir solution and then equilibrated with 50 mL of the 339 340 reservoir solution using a crystallization robot, Mosquito[®] Xtal3. The crystallization conditions were screened using the sparse-matrix sampling method, according to the sitting-drop vapor 341 diffusion method at 20 °C in a 96-well plate (violamo). After a week, well-formed crystals of 342 Anc4 and Anc5 were obtained using PEGRx 1 (Hampton Research) and further optimized to 343 the condition (15% and 27% (w/v) polyethylene glycol monomethyl ether 2,000, 0.1 M MES 344 345 monohydrate pH 6.0 for Anc4 and Anc5, respectively).

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347 X-ray data collection

For data collection, the crystals of Anc4 and Anc5 were soaked in cryoprotectant buffer (40%
(w/v) polyethylene glycol monomethyl ether 2,000, 0.1 M MES monohydrate pH 6.0) for 1
min before flash-cooling to 100K in liquid nitrogen. Diffraction datasets were collected at 100
K on BL32XU or BL41XU beamline of the SPring-8 (Harima, Japan), employing the

automated data collection ZOO⁴². The collected datasets were processed automatically with
KAMO⁴³. Each dataset was indexed and integrated using XDS⁴⁴, followed by a hierarchical
clustering analysis using the correlation coefficients of the normalized structure amplitudes
between datasets. Finally, a group of outlier-rejected datasets was scaled and merged using
XSCALE⁴⁵ or Aimless⁴⁶.

357

358 Structure solution and refinement

General data handling was performed with the Phenix package⁴⁷. The initial model was solved by molecular replacement using Phaser⁴⁸ with the model structure of Anc4 and Anc5 predicted by AlphaFold2⁴⁹. The model building was performed with *Coot*⁵⁰. Structures were refined by *Coot*⁵⁰ and Phaser⁴⁴. The details of crystallization, structure determination, the data collection, data processing, and refinement statistics are given in Supplementary Tables 2 and 3. Structural figures are described and rendered by the PyMOL Molecular Graphics System, Version 1.2r3pre, Schrödinger, LLC.

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367 Molecular Dynamics Simulations

The MD simulations were performed using GROMACS version 2020.1⁵¹ and the charmm36-368 mar2019 force field⁵². The model structure of Anc4+LII and Anc5 Δ LI were built using Anc4 369 370 and Anc5 structures obtained from this work and used as a starting point for MD simulations. For each model, the system was solvated and neutralized with Na⁺ and Cl⁻ ions in a 371 dodecahedral box. Temperature was maintained at 310 K by using a modified Berendsen 372 thermostat⁵³ and pressure was maintained at 1 bar by using a Parrinello-Rahman barostat⁵⁴. 373 374 The system was then equilibrated on energy, temperature, and pressure before performing four individual repeats of 200 ns of the simulations. To analyze the fluctuation, Gromacs standard 375 376 analysis package was used.

377

378 Rigidity-based allosteric communication and FIRST

Allostery analysis was carried out by applying rigidity-transmission allostery (RTA) analysis¹⁶. 379 The RTA method utilizes graph and rigidity theory^{17,18} techniques to identify allosteric 380 networks within structures of proteins and protein complexes¹⁹⁻²². Starting with protein 381 structures of Anc4 + Loop II and Anc5 Δ LoopI, we applied the RTA algorithm by sequentially 382 perturbing rigidity of individual residues and monitoring changes in conformational degrees of 383 384 freedom in loop II. Rigid cluster decomposition and dilution plots on Anc4 + Loop II and Anc5 Δ LoopI were performed with software FIRST²³. FIRST creates a geometric molecular 385 386 framework, whose underlying network (graph) contains atoms (vertices) and edges (*i.e.* constraints representing covalent bonds, hydrogen bonds, electrostatic interactions, and 387 hydrophobic contacts). Every potential hydrogen bond is assigned an energy strength in 388 kcal/mol, and a hydrogen bond cutoff energy value was selected so that all bonds weaker than 389 this cutoff are removed from the network. FIRST then applies the pebble game algorithm^{18,55} 390 391 which rapidly decomposes a protein structure into flexible and rigid regions while incrementally removing weak hydrogen bonds. 392

393 *Microscopic observations*

10 mL of sterilized PDB (Potato dextrose broth) medium containing 10^6 spores/mL of T.*longibrachiatum* was incubated at 25°C for 24 h with shaking at 300 rpm to obtain the mycelia of the fungi. The mycelia were collected by centrifugation (3000*g*, 25 °C, 20 min) and was resuspended by PDB medium. Then, 50 µL of the mycelial suspension was mixed with 50 µL of 2 µM each protein sample solution and incubated at 25 °C for 1 h. The incubated solution mixture was washed three times with 20 mM sodium phosphate buffer (pH 7.4). The samples

- 400 were observed with confocal laser scanning microscopy. Each protein sample was tagged with
- 401 Alexa Fluor 488 Microscale Protein Labeling Kit, followed by the manufacturer's protocol.
- 402 Figures
- 403

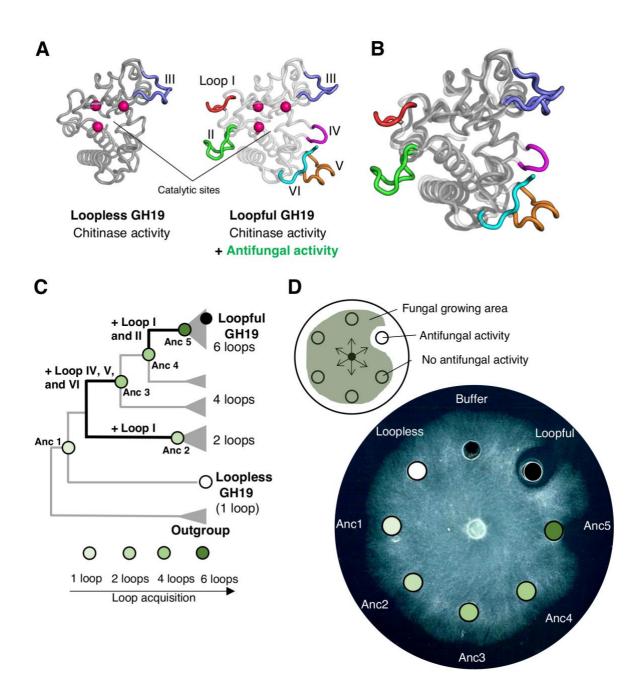
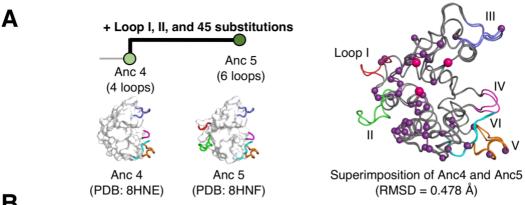


Fig. 1. Antifungal activity is acquired during evolution in GH19 chitinase. A) Structural
 comparison of two types of GH19 chitinase, loopless and loopful. They share the core region

407 (darker and lighter grey in loopless and loopful GH19, respectively), two catalytic glutamic acids, and one serine that holds catalytic water (magenta spheres) but differs in loop regions, 408 named I to VI. (shown in red, green, light blue, purple, orange, and cyan, respectively). B) 409 410 Structural superimposition of loopless and loopful. The detail catalytic mechanism that they 411 conserve is shown in Fig. S1. C) Schematic representation of a phylogenetic tree of GH19 412 chitinase. The five ancestral nodes that were characterized are labeled and colored according 413 to the number of loop regions (80% lighter green, one loop; 60% lighter green, two loops; 40% lighter green, four loops; 25% darker green, six loops). Evolutionary transitions containing 414 415 loop acquisitions are highlighted with thick black lines. A multiple sequence alignment of two 416 modern and five ancestor sequences and a full phylogenetic tree are shown in Figs. S2 and S3, respectively. **D**) Top, a schematic representation of fungal hyphae expansion inhibition assay 417 418 against Trichoderma longibrachiatum as the test fungus. Bottom, the assay plate. Each well contains 10 µL of sterilized buffer (10 mM sodium acetate buffer, pH 5.0) or 500 pmol of 419 protein samples dissolved in the same buffer. 420



B

(Variants	Chitinase activity (U/mol) ×10 ⁹	Antifungal activity (IC ₅₀ , μM)	/ Thermostability (Tm, °C)
Anc 4	1.05	488 ± 3	72.5
Anc 4 + Loop I	N. D.	N. D.	64.0
Anc 4 + Loop II	1.15	$\textbf{737} \pm \textbf{7}$	64.0
Anc 4 + Loop I and	II N. D.	N. D.	55.0
Anc 5	0.85	16.9 ± 1.4	66.0
Anc 5 ∆ Loop I	1.28	17.2 ± 1.9	60.0
Anc 5 ∆ Loop II	1.04	200 ± 20	62.0
Anc 5 \triangle Loop I and	III 1.28	575 ± 4	72.0

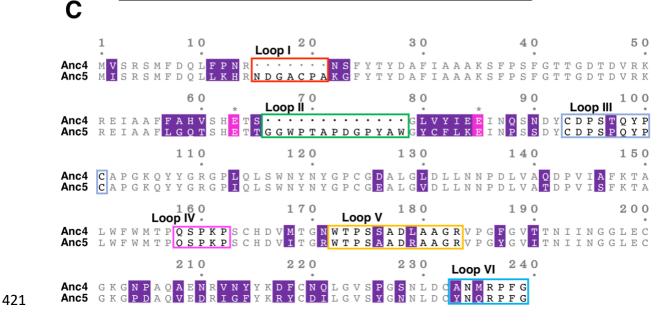
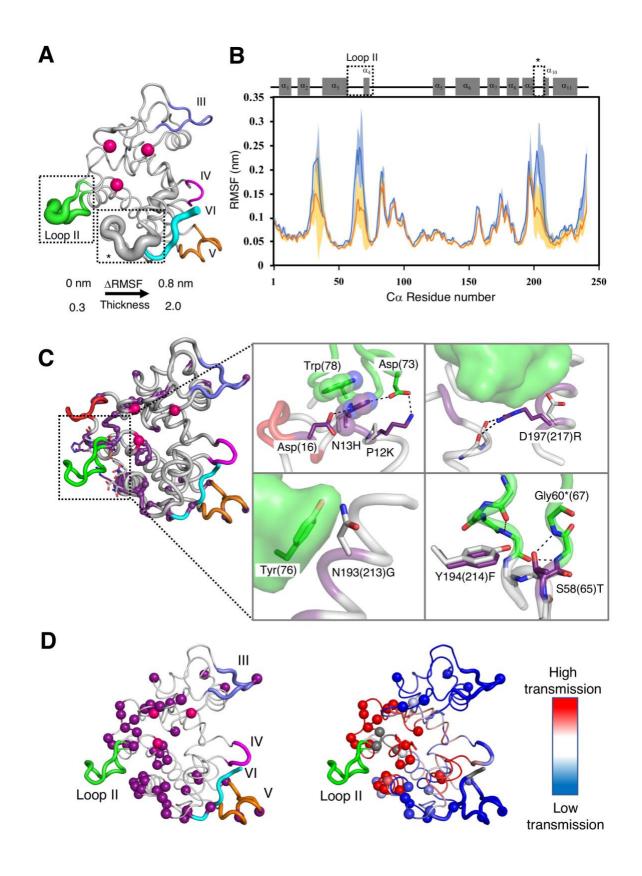


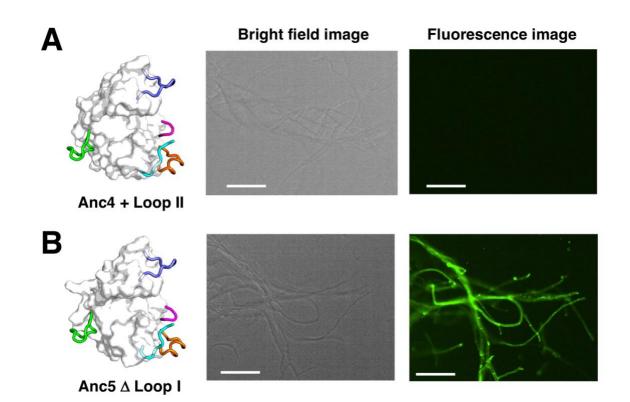
Fig. 2. Characterization of eight variants of two ancestral proteins reveal the key remote 422 loop for the acquisition of antifungal activity. A) Left, a schematic representation of an 423 evolutionary transition from Anc4 to Anc5. Crystal structures of Anc4 and Anc5 solved to 1.13 424

Å and 1.57 Å, respectively. Right, structural superimposition of Anc4 and Anc5. Two catalytic 425 426 glutamic acids and one serine reside that holds catalytic water are indicated as magenta spheres. 45 substitution residues are indicated as purple spheres. **B**) Summary of the effects of loop 427 428 presence/absence on the hydrolytic and antifungal activities. One unit of activity is defined as 429 the enzyme activity that produced one µmol of GlcNAc per minute at 37°C. Error bars represent SD (n = 3). Melting temperature (T_m) was measured using differential scanning 430 fluorimetry followed by the procedures as described in the Methods. C) An alignment of Anc4 431 432 + Loop II and Anc5 \(Loop I sequence. Loop regions II to VI are highlighted in green, light blue, purple, orange, and cyan squares, respectively. Two glutamate residues and one serine 433 434 residue are shown in magenta. 45 substitutions residues are shown in purple.



436 Fig. 3. Comparison of Anc4 + Loop II and Anc5∆Loop I exhibit the structural and
437 dynamics contribution of Loop II and scaffold substitutions. A) The difference in ∆root

mean square fluctuation ($\Delta RSMF = RMSF$ of Anc4 + Loop II - RMSF of Anc5 Δ Loop I) is 438 439 mapped on the structure of Anc5 Δ Loop I as the thickness of the cartoon representation. Spheres indicates two catalytic glutamic acids and one serine that holds catalytic water. **B**) Plots of the 440 RMSF of C α of each residue in Anc4 + Loop II (blue) and Anc5 Δ Loop I (orange). Error bars 441 are indicated as shades. A schematic representation of secondary structures of GH19 chitinase 442 443 is shown. Dashed squares indicate the region where $\Delta RSMF$ is more than 0.05 nm C) Cartoon tube representation of Anc5. Sphere representation indicates 45 substitution residues 444 445 (purple) and two catalytic glutamic acids and one serine that holds catalytic water (magenta). Resides around 4 Å from loop II are shown in sticks. Intra molecular interactions stabilizing 446 447 loop II regions are shown in the enlargements. Resides in Anc4 and Anc5 state are shown in 448 grey and purple sticks, respectively. Black dashed lines indicate hydrogen bonds. Residue 449 numbers are based on Anc4. In the case that the number shifts due to loop insertions, residue 450 numbers of Anc5 state are in parentheses. An asterisk indicates the number of Anc4 + Loop II. 451 Loop regions I to VI are shown in red, green, light blue, purple, orange, and cyan, respectively. D) Left, computational analysis of long-range communication in Anc5∆Loop I. Cartoon 452 453 representation of Anc5 Δ Loop I with cartoon_tube representation of loop II to VI (shown in green, slate, purple, orange, and cyan, respectively). Sphere representation indicates 45 454 455 substitutions residues (purple) and two glutamic acids and one serine that holds catalytic water 456 (magenta). Right, rigidity transmission allostery (RTA) communication analysis on 457 Anc5∆Loop I. Residues are colored based on the intensity (red being highest) of long-range 458 rigidity transmission communication with loop II (green). Spheres indicate 45 substitutions.



459

460 Fig. 4. Fluorescence microscopy images of fluorophore-labelled protein Anc4 + Loop II
461 and Anc5ΔLoop I on the surface of fungal hyphae reveal the mechanism of acquisition of
462 antifungal activity.

463 Each 50 µL of 2 µM Alexa Fluor 488-labelled proteins Anc4 + Loop II and Anc5 \(\Loop I) is 464 mixed with T. longibrachiatum hyphae in 20 mM sodium phosphate buffer, pH 7.4 at 25 °C. Images were captured after washing excess of the labelled proteins. All scale bares are 100 µm. 465 466 A) From left to right: the structure of Anc4 + Loop II; Bright field image of fungal hyphae; Fluorescence microscope image shows no binding to the surface of fungal hyphae. B) From 467 468 left to right: the structure of Anc5 + Loop II; Bright field image of fungal hyphae; Fluorescence microscope image shows Alexa Fluor 488-labelled Anc5 ALoop I binding to the surface of 469 470 fungal hyphae.

472 Table 1 Enzymatic activities and melting temperature of the two modern and five ancestral GH19

473 chitinases

Protein	Loop	Specific activity	DSF
		$(U^*/mol) \times 10^9$	T _m (°C)
Anc1	III	1.44	58.5
Anc2	I and III	0.75	52.0
Anc3	III, IV, V, and VI	1.20	72.0
Anc4	III, IV, V, and VI	1.05	72.5
Anc5	I, II, III, IV, V, and VI	0.85	66.0
Loopless	III	1.51	68.0
Loopful	I, II, III, IV, V, and VI	0.83	62.5

* One unit of activity is defined as the enzyme activity that produced one μmol of GlcNAc per
minute at 37°C. Melting temperature (T_m) was measured using differential scanning
fluorimetry (DSF) followed by the procedures as described in the Methods.

477

478 Acknowledgments

Financial support by Okinawa Institute of Science and Technology (OIST) is gratefully 479 480 acknowledged. We thank Nobuhiko Tokuriki for the discussion on the project. We thank Toki Taira, and Ben Clifton and Erika Fukuhara for their insightful comments on this manuscript. 481 We are grateful for the help provided by the scientific computing, the Data Analysis, and the 482 483 Instrumental sections at OIST. We also thank Paolo Barzaghi from the Imaging Section of OIST for the help with microscope experiments and Stefano Pascarelli for assistance with 484 485 molecular dynamics simulations. The synchrotron radiation experiments were performed at BL45XU and BL41XU of SPring-8 with the approval of the Japan Synchrotron Radiation 486 487 Research Institute (JASRI) (Proposal No. 2022A2769)

489 Author contributions

- 490 D.K. and P.L. designed the project. D.K. performed phylogenetic analysis, all the biochemical
- 491 experiments, biophysical characterization of all the proteins and mutants, fluorescent imaging
- 492 microscope experiments, and molecular dynamics simulations. A.S. performed rigidity-
- 493 transmission allostery computation and the related data analysis. D.K. and P.L. wrote the
- 494 manuscript with the input from A.S. This project was supervised by P.L.

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